

**SCIENTIFIC REPORT**  
**on the project “Global Bifurcation Analysis of**  
**Biomedical and Ecological Rational Dynamical Systems”**  
**supported by the IMU-Simons Foundation**

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- **Research in progress:**
  1. Developing our bifurcational geometric approach, we solve the limit cycle problem for the general Liénard polynomial system.
  2. Using a similar approach and some numerical results, we present a new scenario of chaos transition for the classical Lorenz system.
  3. We complete the global qualitative analysis of a quartic family of planar vector fields corresponding to a rational Holling-type dynamical system which models the dynamics of the populations of predators and their prey in a given ecological or biomedical system.
- **Papers published or in preprint form:**
  1. V.A.Gaiko, Bifurcation analysis of Liénard and Lorenz polynomial dynamical systems, submitted to the journal of *Dynamical Systems: An International Journal*, 11 p.
  2. V.A.Gaiko, The maximum number of limit cycles in a Holling type dynamical system, submitted to the journal of *Nonlinear Analysis: Real World Applications*, 12 p.
  3. V.A.Gaiko, Global bifurcations of limit cycles in a Holling-type dynamical system, *arXiv:math.DS/150403353*, 2015, 19 p.
- **PhD students advised:** Sabrina Streipert, Nasrin Sultana, Tom Cuchta, Gülşah Yeni, Ismail Tiryaki.
- **Dates spent at the university:** 02.03.2015–29.04.2015.

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