



# The Italian Didactic Tradition

Specific features of the Italian situation and salient aspects of Mathematics education in the Italian cultural context

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A look at the past

# The situation

1970s - 80s in Italy – consolidated tradition of cooperation between universities and schools  
(**mathematicians**: e.g. Giovanni Prodi, Lucio Lombardo Radice, Francesco Speranza);  
(**teachers**: e.g. Emma Castelnuovo, to whom the International ICMI award for outstanding achievements in the practice of mathematics education is dedicated)


# The situation

## Teacher-researchers


Members of mixed groups at the main  
Universities,

with habit of parithetic cooperation  
with academics

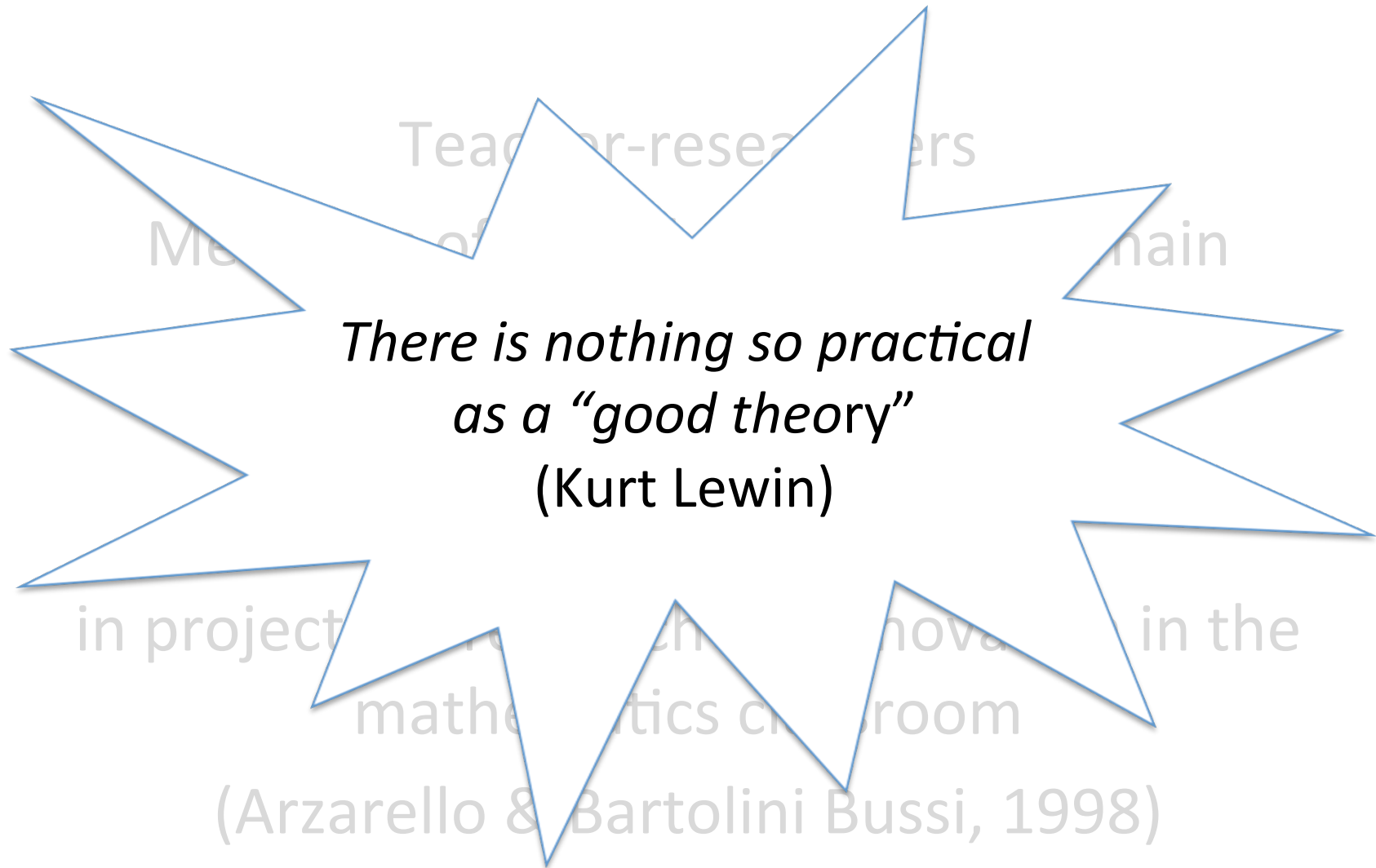
in projects of research for innovation in the  
mathematics classroom



Needs from school  
practice  
(the “local” context)



Needs from academic  
tradition  
(Mathematics;  
Research as  
“international”  
dialogue)



*There is nothing so practical  
as a “good theory”*  
(Kurt Lewin)

(Arzarello & Bartolini Bussi, 1998)

# Teacher-researchers' needs 1970s .....

To focus on:

- **Whole class interaction** (beyond the more popular studies on individual problem solving and small group cooperative learning)
- **The teacher's role as a guide** (beyond the more popular focus on learner's processes)
- **Long term processes** (beyond the more popular studies on short term processes)
- **Manipulation of concrete artifacts (e.g. abacus, curve drawing devices, tools for perspective drawing)** without overlooking the theoretical aspects of mathematical processes

# A look at the past

This situation was summarized in the 90s:

1994-98

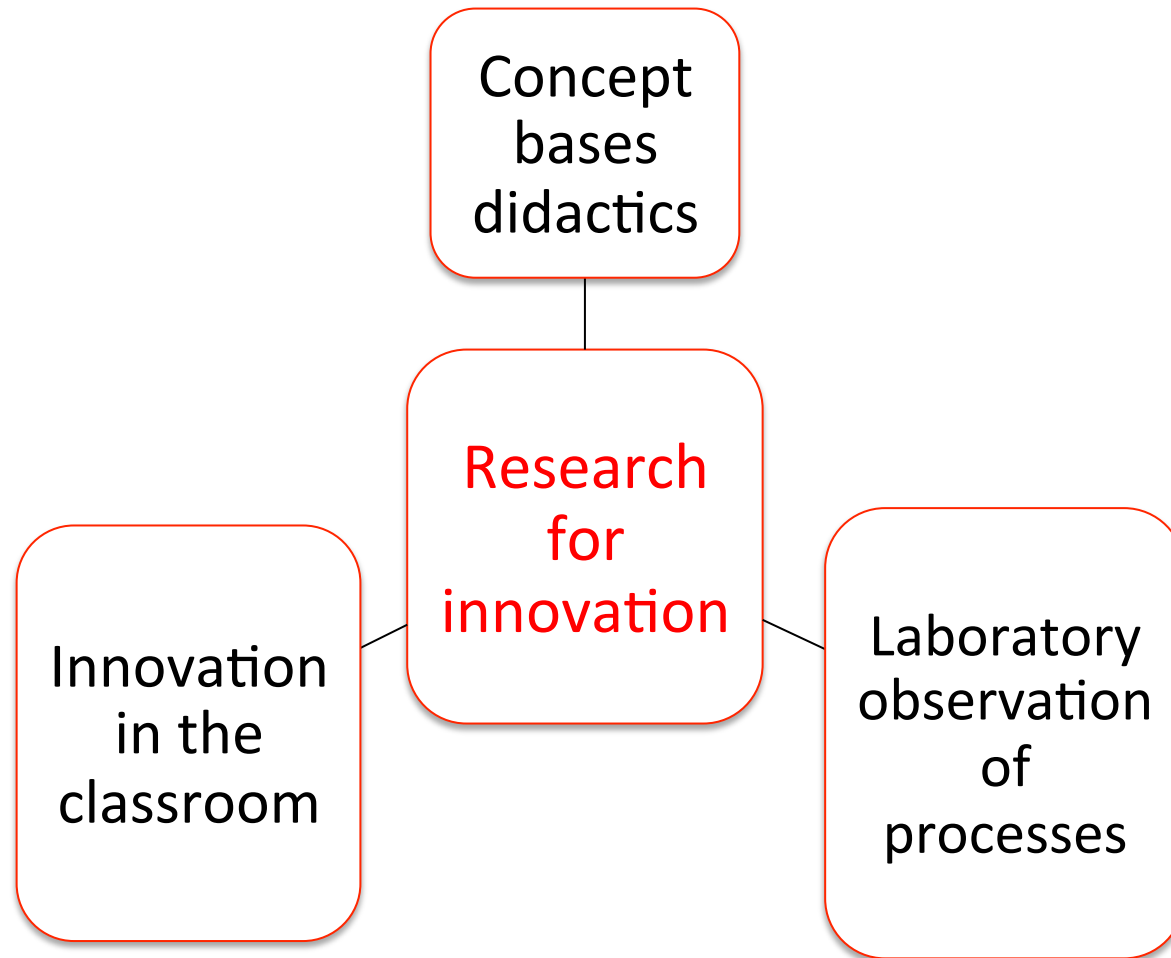
F. Arzarello & M. Bartolini Bussi

(ICMI Study n. 8)

*Italian trends in research in mathematical education: a national case study from an international perspective*



# A systemic view



# A dynamic analysis

- **Minimality test.** In a research study in mathematics education at least two of the three components ... are considered. Relevance requires that all three of the components ne considered.
- **Dynamic interfunctionality test.** In a research study in mathematics education .... analysis is focused on the mutual relationships between the components rather than on the components themselves.
  - (FA & MBB, 1998)

# Thirty years later

This systemic approach is still fundamental, although

- additional components have strongly emerged (e.g. the study of beliefs and conceptions)
- the landscape is changed (e.g. the impact of technologies; the attention to students with special needs; the major issue of teacher education; the awareness of multicultural aspects)

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# In the past

teacher-researchers  
in the parithetic  
collaboration between  
academics and teachers

research models  
(and findings)  
with strong links with  
school needs and  
constraints

But

the optimistic **illusion** in  
the gradual expansion to  
schools  
(**teacher education and  
development**)

# The recent history of teacher education in Italy

## Pre-primary and primary school

University programs (masters)

from 1998 (4 years)

From 2010 (5 years)

with strong balance between

Courses (psyco-peda area + subject matters)

Practicum

Workshops

## Secondary school

1999-2009 nine cycles of 2 year specialization after master degrees (e. g. in Mathematics)

2011- today? 1 year specialization after master degrees

Now: reform???

# The situation is very different

## Pre-primary and primary school

A “quiet and safe” development of good practices and studies without solution of continuity since 1998;  
Stronger and stronger links between general education and disciplines  
(Mathematics, Science, language ...)

## Secondary school

A continuously interrupted process with tensions and difficult relationships between general educators and specialists of disciplines

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2015: A reform  
La buona scuola - The good school was issued.  
A comprehensive programme of teacher education and development is debated



# The recent history of teacher development in Italy

**La buona scuola** has for the first time transformed in service teacher development into a:

- compulsory
- sistematic
- funded

activity

but the details are still unknown and the role of Universities (beside other private agencies, trade unions ad similar) is not yet clear.

# A personal example

The two early research projects  
developed with teachers-researchers  
(PME 33 – 2009)

Vygotskian approach  
to social interaction

**Mathematical  
Discussion**

orchestrated by the  
teacher.

Several teaching  
experiments  
(grades 1-8)  
(PME PL -15 - 1991)

Instrumental approach  
to Mathematical Laboratory

**Mathematical Machines  
(concrete instruments)**

Construction and didactical  
use.

Several teaching  
experiments  
(initially, grades 9-13)  
(PME RR - 17 - 1993)

# Implementation in teacher education and development

Larger and larger dissemination of this  
methodology drawing on

international Lesson Study

(especially in the form of the Chinese open-class  
approach)-

**Strong points**

# The effects on the institutional processes in Italy

Mathematical Discussion

Mathematical Laboratory  
with the paradigmatic  
example of **Mathematical  
Machines** next to ICTs

These two theoretical constructs were adopted  
in the methodology background  
**of the Mathematics Curricula**  
prepared by the Italian Mathematical Union /  
Italian Commission on Mathematical Instruction,  
**on behalf of the Ministry of Education**  
and had a strong influence on the national standards  
**issued by MoE (2007 – 2012 - ....)**

# The effects on the institutional processes in Italy

Mathematics Teacher Education and Development

Books for the Italian teachers

Courses / workshops

for pre-service and in-service teacher education

and so on

# The findings for the academic international audience

The development in cooperation with M. A. Mariotti and with many teacher-researchers of a comprehensive and developing theoretical framework on **semiotic mediation in the mathematics classroom after a Vygotskian approach** that encompassess dozens of **teaching experiments in ALL grades** (from pre-school to university teacher education) and **many different artifacts** (from texts and sources and historical instruments to contemporary ICTs)



# The products for the academic international audience

Dozens of research papers  
mainly by Bartolini Bussi, Mariotti and collaborators  
on the main journals of the field  
(ESM, JMTE, ZDM, FLM...)  
on many international volumes and handbooks  
Invitations  
as keynote speakers in International Conferences  
as invited speakers in doctoral schools, summer or winter  
schools, universities, learned societies  
national scientific events in many countries ....  
as members of IPCs of International Conferences  
and ICMI Studies ....

**But ...**

**Weak points**

## At the national level

Slow dissemination out of the research groups to develop teachers' attitudes and beliefs.

# At the international level: theoretical framework

Some of the background choices  
(e.g. the focus on

- the epistemology of mathematics
- the teacher's role as a guide

in the mathematical classroom processes)  
made and make this theoretical framework  
for (Western) researchers less appealing  
than other approaches more biased by  
non-mathematical issues  
(e.g. sociological, psychological)

# An example: teacher's actions in the mathematics classroom

**Negotiation** of meanings, of socio-mathematical norms, development of **taken-as-shared** meanings

(Voigt, Bauersfeld, Steinbring, Cobb et al. ....)

These positions draw on a more or less radical vision of constructivism, where the focus is on the individual learners, as more or less isolated subjects, with a more or less explicit separation from the historic-cultural context.

# An example: teacher's actions in the mathematics classroom

The very formulation of teacher's actions is often more related to general interaction rules (studied in general education) than to the specific mathematical task:

- To invite students
- To establish connections ....

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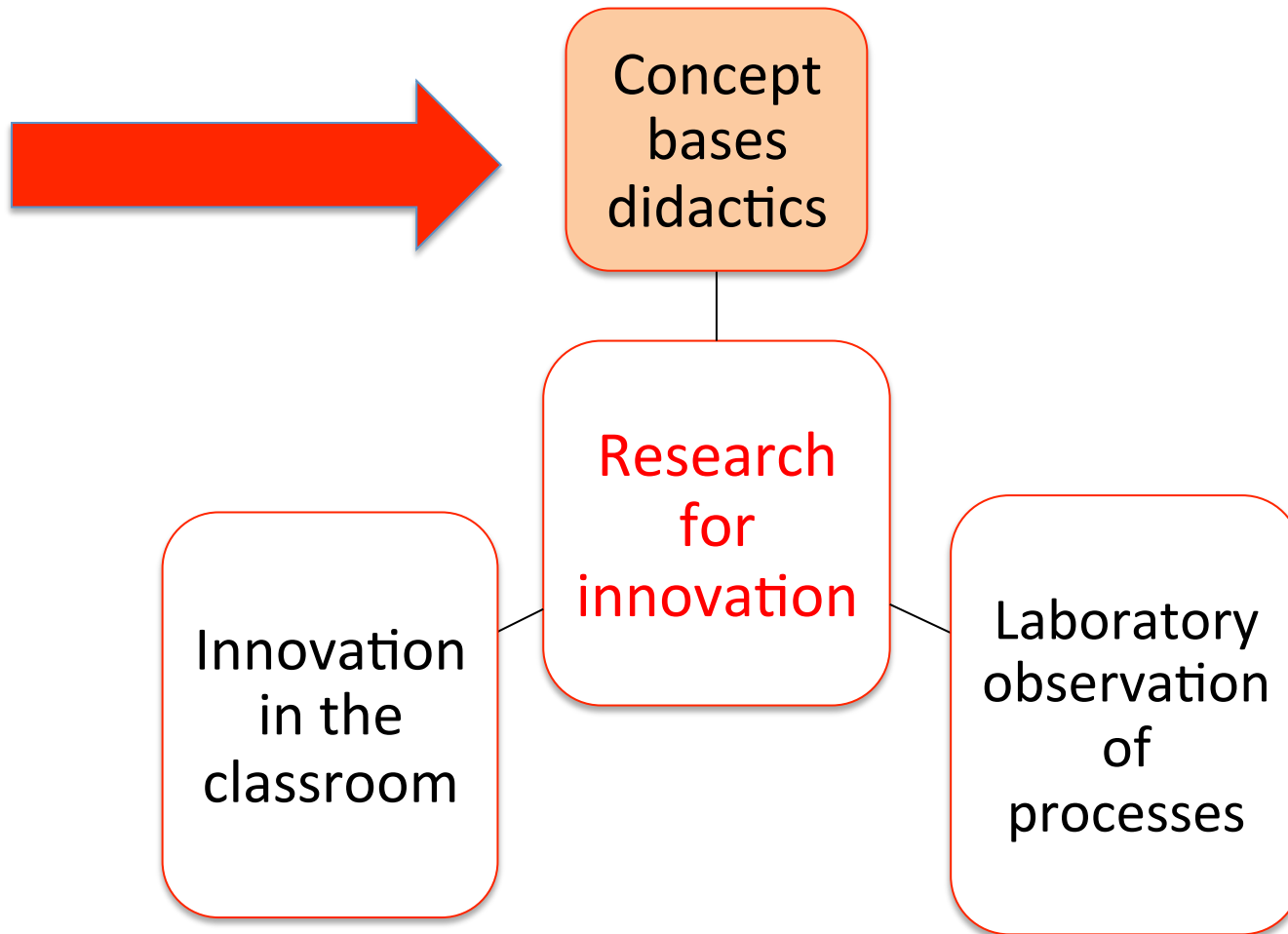
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- To invite students
- To establish connections ....

We too draw on this literature, but ...

- Where is the **specificity of the piece of mathematics knowledge** into play? Of the particular **task**? Of the **artifact(s)** to be used?
- Are there differences between **mathematical discussions** and philosophical discussions (e.g. the more and more popular approaches to philosophy for children)?

# A systemic view





**Hopes**

# Advantages of this theoretical framework

Some of the background choices,

e.g. the focus on

- the epistemology of mathematics
- the teacher's role as a guide

in the mathematical classroom processes,

are consistent with **the systems of values** developed in some large regions of the global world,

showing themselves only recently in the forum of mathematics education

(e.g. Far East regions; developing countries)

# A finding from a very large international study: the Learner's Study

Whether we look to  
the Japanese  
“gakushushido” - 学 (Chinese “xuè”)  
the Dutch  
“leren”  
or the Russian  
“obučenie” - обучение  
we find that some communities have acknowledged the  
interdependence of **instruction** and **learning** by  
encompassing both activities within the one process and,  
most significantly, within the one word.  
In English, we seem compelled to dichotomise classroom  
practice into Teaching or Learning.

(D. Clarke)

# Advantages of this theoretical framework

This theoretical framework may create the conditions for a fruitful and effective international dialogue not limited to the so-called Western countries

# Personal experiences

- Strong connections with Far East communities of mathematics educators (Japan, China, Thailand, Myanmar-Burma and so on)
- A project with Japan (Masami Isoda, Tsukuba Univ. Japan)
- An ongoing joint project with Macau-China (Sun Xuhua, University of Macau)
- A planned project on mathematics teacher education with Burma (NLD – Aung San Suu Kyi party)
- The extraordinary experience of co-chairing the first ICMI study on primary school (ICMI Study 23) with a very strong IPC coming from all the 5 continents.

# A personal wish/dream

To educate Italian and European future teachers and future researchers in mathematics education (e. g. doctoral students) to an open minded approach, with the awareness that

- one's own cultural values mould one's own research studies, that are contextually-dependent;
- findings of research studies are themselves contextually-dependent;
- even analytical tools are themselves contextually-dependent.

No finding, no artefact, no analytical tool may be shifted from one context to another without a previous careful analysis, i. e.  
a process of “cultural” transposition  
from a country to another.

(Bartolini Bussi et al., FLM, 2013 and 2014)



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**Thank you!**

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